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FACULTY OF ENGINEERING AND TECHNOLOGY

DEPARTMENT OF ELECTRICAL AND COMPUTER ENGINEERING

ENEE 4113

communication Laboratory.

Experiment 1

AM Modulation and Demodulation

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Section # : 3

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❖ Part 1: Normal AM in the time and frequency domain:

In Normal AM, the formula of the modulated signal is shown below:

$$S(t) = A_c(1 + K_a m(t))\cos 2\pi f_c t$$

Where:

S(t): The modulated signal.

m(t): The modulating signal (message signal). A_c: The amplitude of the carrier signal.

f_c: The frequency of the carrier signal.

K_a: Constant that represents the modulation sensitivity.

The envelope of S(t) is defined as:

$$A(t) = |A_c (1 + K_a m(t))|$$

The message signal is :

$$m(t) = A_m \cos 2\pi f_m t$$

Where:

m(t): message signal.

A_m: The amplitude of the message signal.

f_m: The frequency of the message signal.

- Notice that the envelope of s(t) has the same shape as m(t) provided that it must be positive for a distortion-less demodulation using coherent detector.

Let :

$A_m = 1$ # amplitude of message signal

$F_m = 1000$ # frequency of message signal

$A_c = 1$ # amplitude of carrier signal

$F_c = 10000$ # frequency of carrier signal

$K_a = 0.5$ # amplitude sensitivity

$$m(t) = 1 \cdot \cos(2\pi(1000)t)$$

$$c(t) = 1 \cdot \cos(2\pi(10000)t)$$

$$s(t) = 1[1 + 0.5 \cdot 1 \cdot \cos(2\pi(1000)t)] \cos(2\pi(10000)t)$$

The signals were plotted in time and frequency domain as shown in fig below

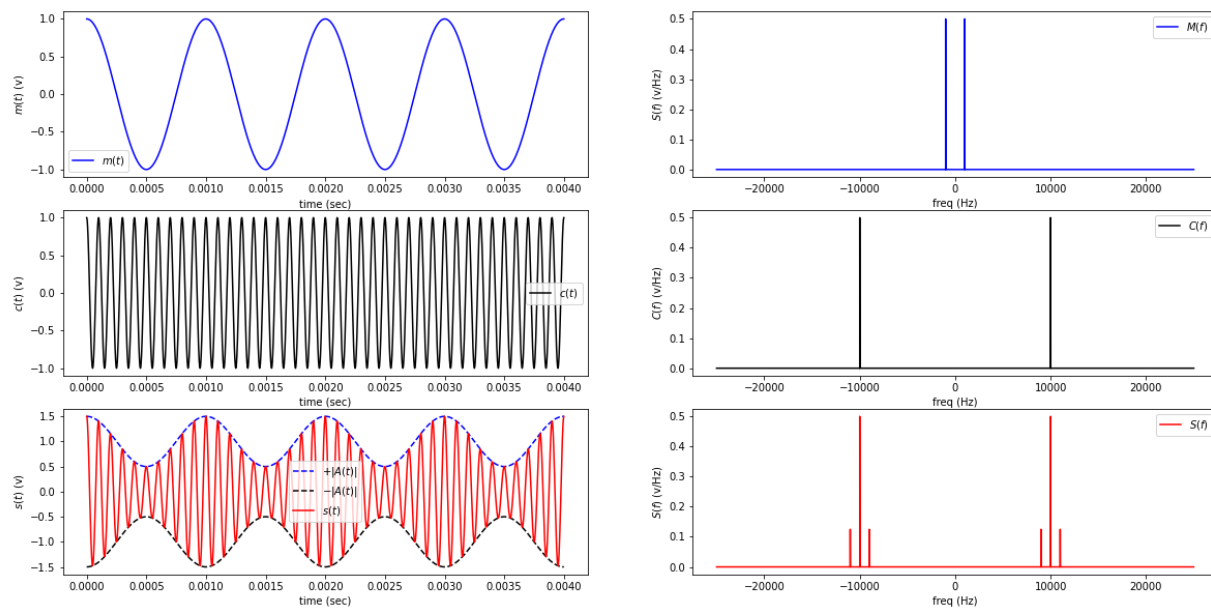


Figure 1: $m(t)$, $c(t)$, $s(t)$ in time and frequency domain

- **Note:** We notice 3 signal in the above figure, $m(t)$ -message-, $c(t)$ - carrier - each with a different shape, amplitude and frequency. $S(t)$ –AM modulation signal- signal That depend on $m(t)$ and $c(t)$.

Exercise:

The parameters of the signal were varied as following

1- $f_m = 500$ Hz

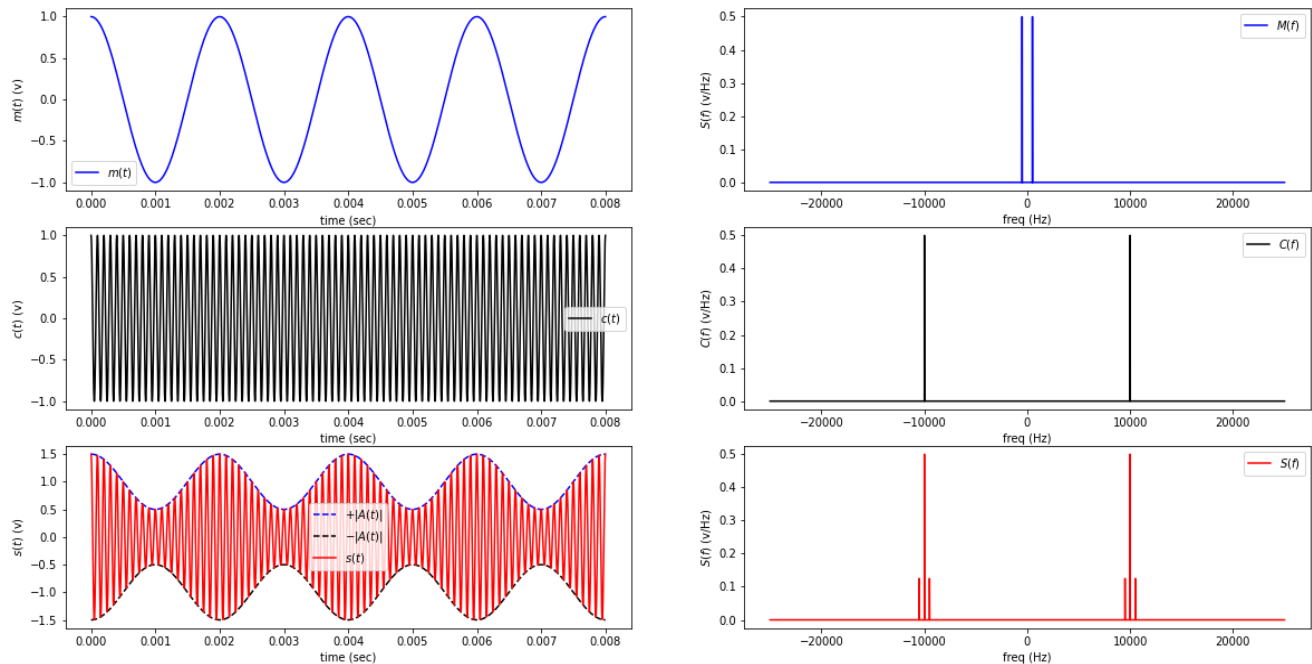


Figure 2: $m(t)$, $c(t)$, $s(t)$ in time and frequency domain with $f_m = 500$

- **Note:** when f_m was decreased/increase the waves for message change . also carrier envelop and AM signal close together if decreased or move away from each other if increase . in addition to the AM signal frequency changed by

$$(f_c - f_m, f_c, f_c + f_m) \Rightarrow (10000 - 500, 10000, 10000 + 500)$$

$$(-f_c - f_m, -f_c, -f_c + f_m) \Rightarrow (-10000 - 500, -10000, -10000 + 500)$$

But carrier frequency doesn't change.

2- $f_c=5000$ Hz :

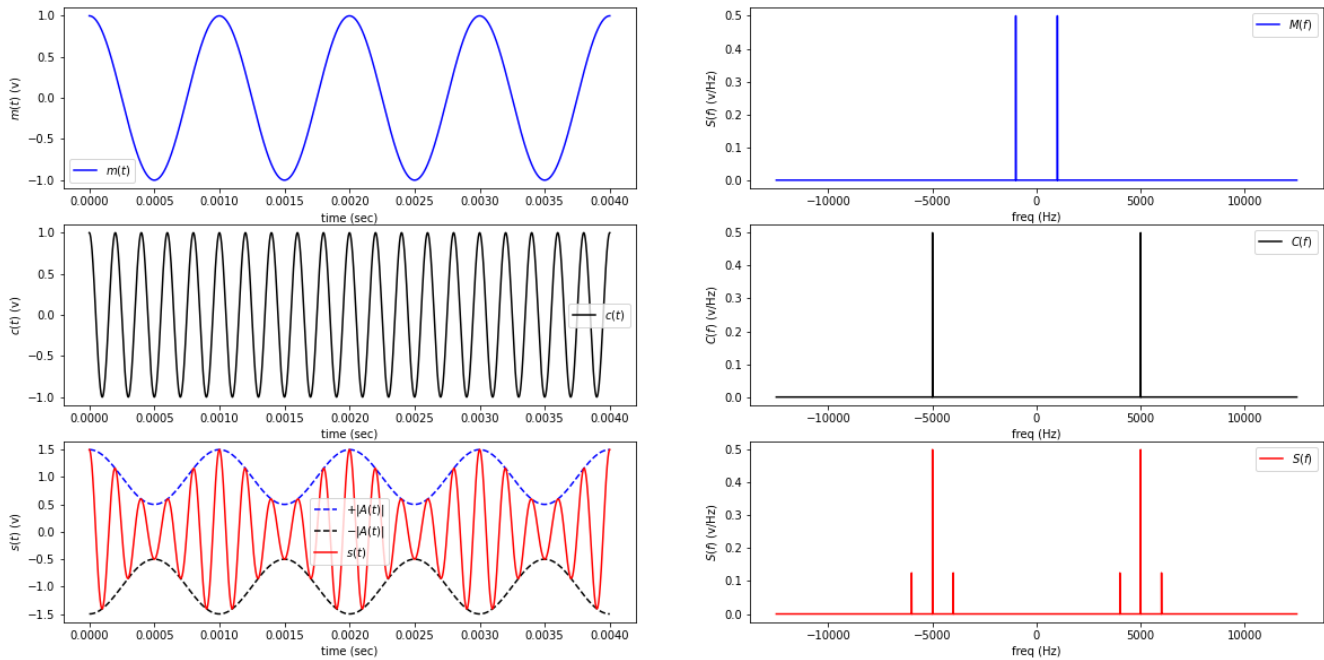


Figure 3: $m(t)$, $c(t)$, $s(t)$ in time and frequency domain with $f_c = 5000$

- Note:** when f_c was decreased/increase the envelop and frequency of message signal were not affected . but waves for carrier envelop and AM signal waves expand and move away from each other if decreased or close together if increase.

And the AM signal frequency changed by :

$$(f_c - f_m, f_c, f_c + f_m) \Rightarrow (5000 - 1000, 5000, 5000 + 1000)$$

$$(-f_c - f_m, -f_c, -f_c + f_m) \Rightarrow (-5000 - 1000, -5000, -5000 + 1000)$$

3- $A_m = 2$:

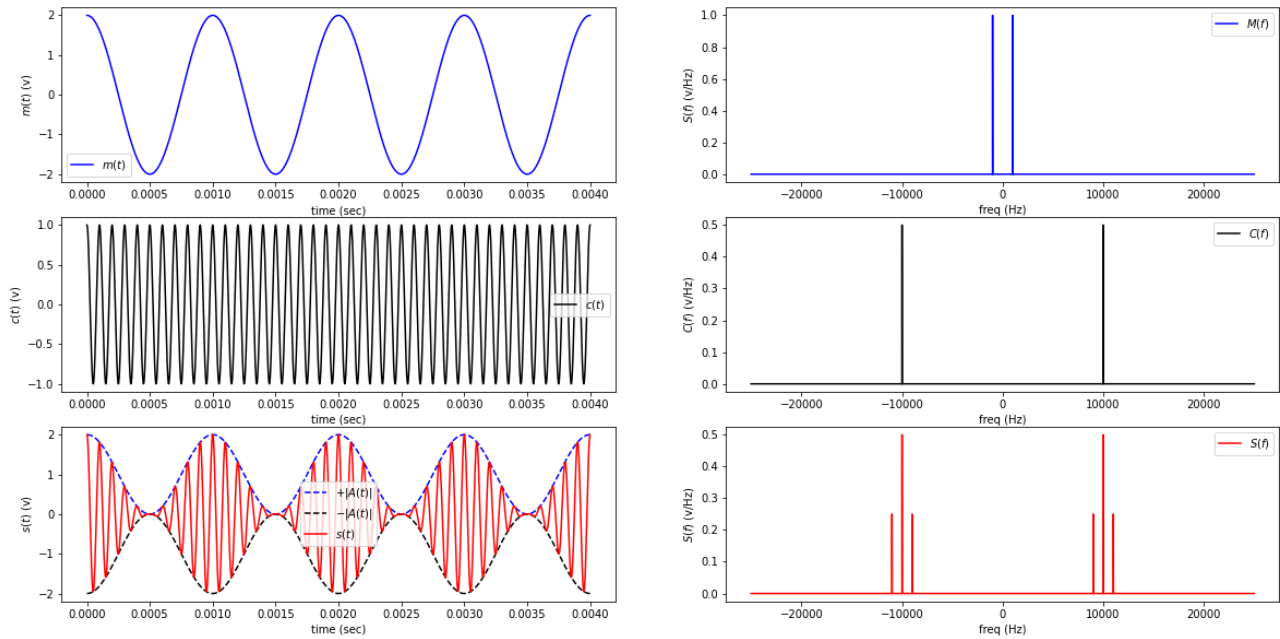


Figure 4: $m(t)$, $c(t)$, $s(t)$ in time and frequency domain with $A_m = 2$

- Note:** when A_m increased/decreases the peak of the message increases and AM signals envelope increases/decreases by $(A_c + (A_c \cdot A_m \cdot K_a))$. In addition to, message amplitude frequency value changes by $(A_m/2)$ also for the upper and lower parts in AM frequency change by $(A_m \mu/4)$. But the carrier envelope and frequency were not affected.

4- $A_c = 2$

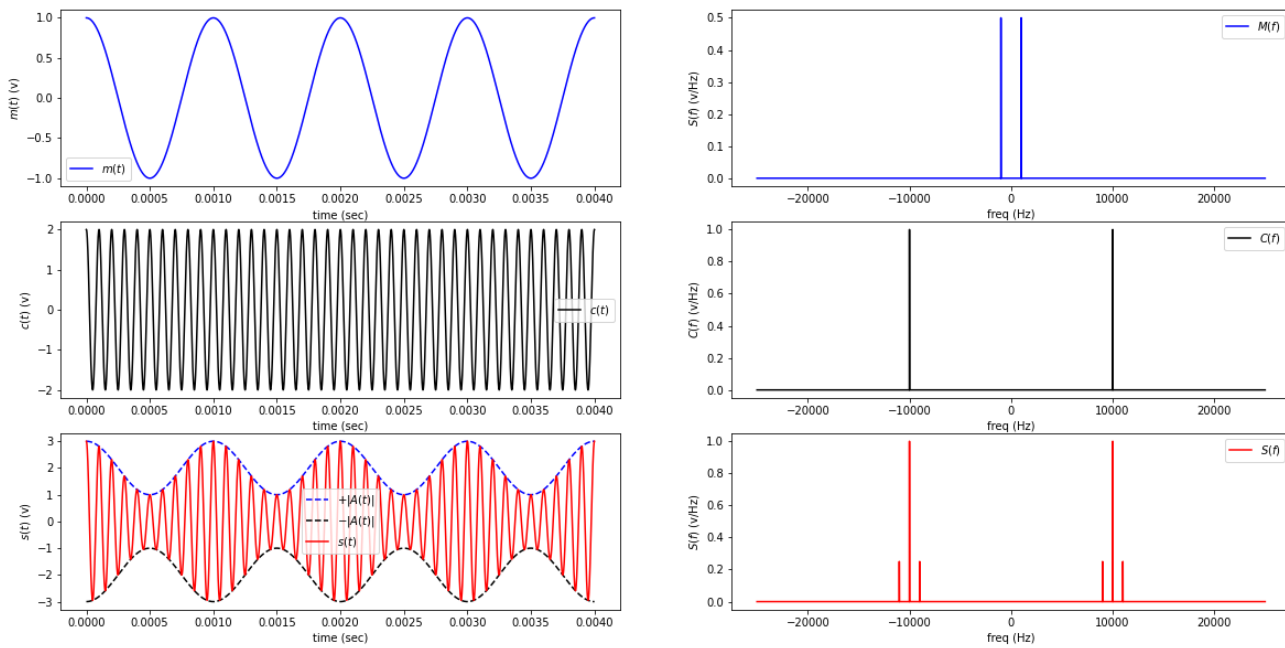


Figure 5: $m(t)$, $c(t)$, $s(t)$ in time and frequency domain with $A_c = 2$

- Note:** when A_c increased / decrease the peak of the carrier increases / decrease and AM signals envelope increases / decrease by $(A_c + (A_c \cdot A_m \cdot K_a))$. in addition to, carrier amplitude frequency value changes by $(A_c/2)$. But the message envelope and frequency doesn't change

5- $K_a=1$:

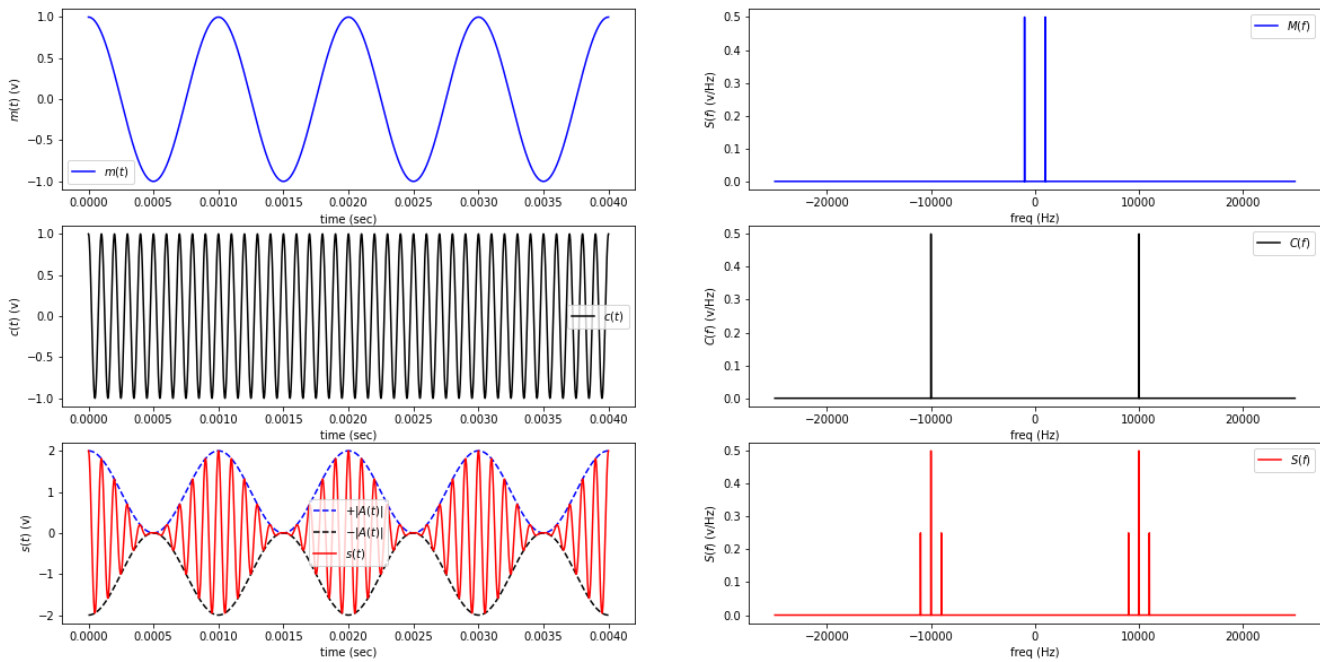


Figure 6: $m(t)$, $c(t)$, $s(t)$ in time and frequency domain with $K_a = 1$

- **Note:** when K_a increased/decreases the carrier and message signals were not affected but AM signals envelope increases/decrease by $(A_c + (A_c \cdot A_m \cdot K_a))$.

❖ Part 2: The effect of changing the AM modulation index μ :

Then a new constant called The modulation index will appear:

$$\mu = Ka Am$$

where:

μ : modulation index , $0 < \mu < 1$

Ka: amplitude sensitivity

Am: amplitude of message signal

There are three cases depending on the modulation index (μ):

- 1- Under modulation when $0 < \mu < 1$
- 2- Over modulation when $\mu > 1$
- 3- Full modulation when $\mu = 1$

Let:

Am1=0.5 # amplitude of first message signal

Am2=1 # amplitude of second message signal

Am3=3 # amplitude of third message signal

fm=1000 # frequency of message signals

Ac=2 # amplitude of carrier signal

fc=10000 # frequency of carrier signal

Ka=1 # amplitude sensitivity

The signals were plotted in time and frequency domain as shown in fig below.

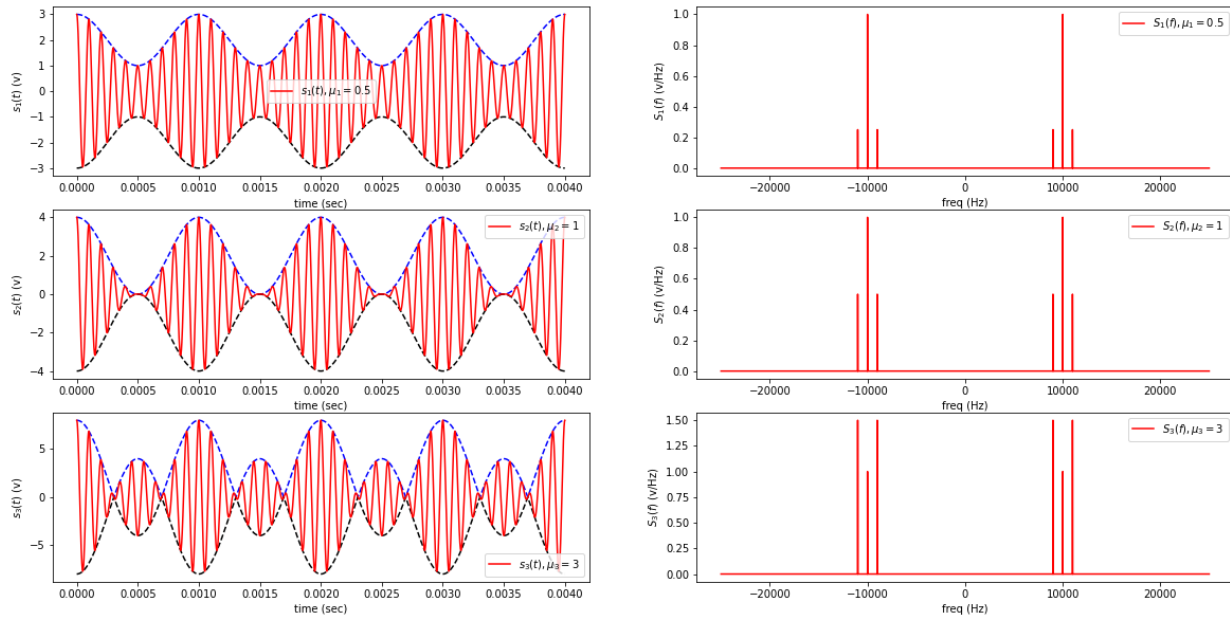


Figure 7: $s(t)$ in time and frequency domain with varied A_m

● **Note:**

- 1- the first figure from the above figure, its under modulation signal and this occurs when $0 < \mu < 1 (\mu = 0.5)$. the envelope is represents message signal. And the power loss between the amplitudes (0.5 and 0) in this case
- 2- the second figure from the above figure, its Full modulation signal and this occurs when $\mu = 1$. the envelope is represents message signal. And the power losses here is less than the under modulation case
- 3- the second figure from the above figure, its over modulation signal and this occurs when $\mu > 1$. In addition to an ideal envelop detector cannot be used to extract $m(t)$ and distortion takes place.

Exercise:

1- $A_{m1}=0.3$, $A_{m2}=0.6$ and $A_{m3}=0.5$ $K_a=2$

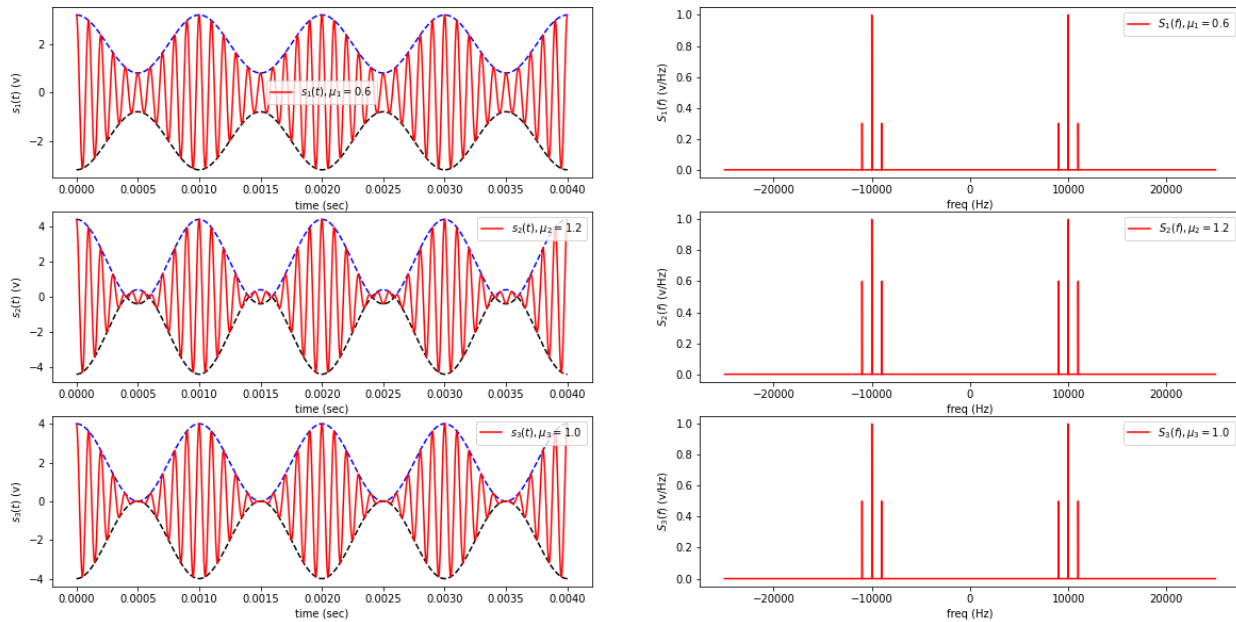


Figure 8: $s(t)$ in time and frequency domain with varied $A_{m1}=0.3$, $A_{m1}=0.6$, $A_{m1}=0.5$, $K_a=2$

- **Note:** the over modulation occurs at $\mu > 1$ which will change the envelope of the message signal and should be avoided . Also, when $\mu = 1$, the envelope is represents message signal.

❖ Part3: Normal AM modulation of a message signal with multiple harmonics:

$$f(t) = A_{m1} \cos(2\pi f_{m1}t) + A_{m2} \cos(2\pi f_{m2}t) + A_{m3} \cos(2\pi f_{m3}t)$$

where:

f(t): sum of 3 cos.

A_{m1,2,3}: amplitude of message signal.

f_{m1,2,3}: frequency of message signal.

$$S(f) = (A_{m1} \cdot A_c / 2) \cos(2\pi(f - f_{m1})t) + (A_{m1} \cdot A_c / 2) \cos(2\pi(f + f_{m1})t) + (A_{m2} \cdot A_c / 2) \cos(2\pi(f - f_{m2})t) + (A_{m2} \cdot A_c / 2) \cos(2\pi(f + f_{m2})t) + (A_{m_n} \cdot A_c / 2) \cos(2\pi(f - f_{m_n})t) + (A_{m_n} \cdot A_c / 2) \cos(2\pi(f + f_{m_n})t) + A_c \cos(2\pi f_c t)$$

Let:

A_{m1}=3 # amplitude of message signal

f_{m1}=1000 # frequency of message signal

A_{m2}=2 # amplitude of message signal

f_{m2}=2000 # frequency of message carrier signal

A_{m3}=1 # amplitude of message signal

f_{m3}=3000 # frequency of message signal

A_c=1 # amplitude of carrier signal

f_c=10000 # frequency of carrier signal

K_a=0.3 # amplitude sensitivity

The signals were plotted in time and frequency domain as shown in fig below.

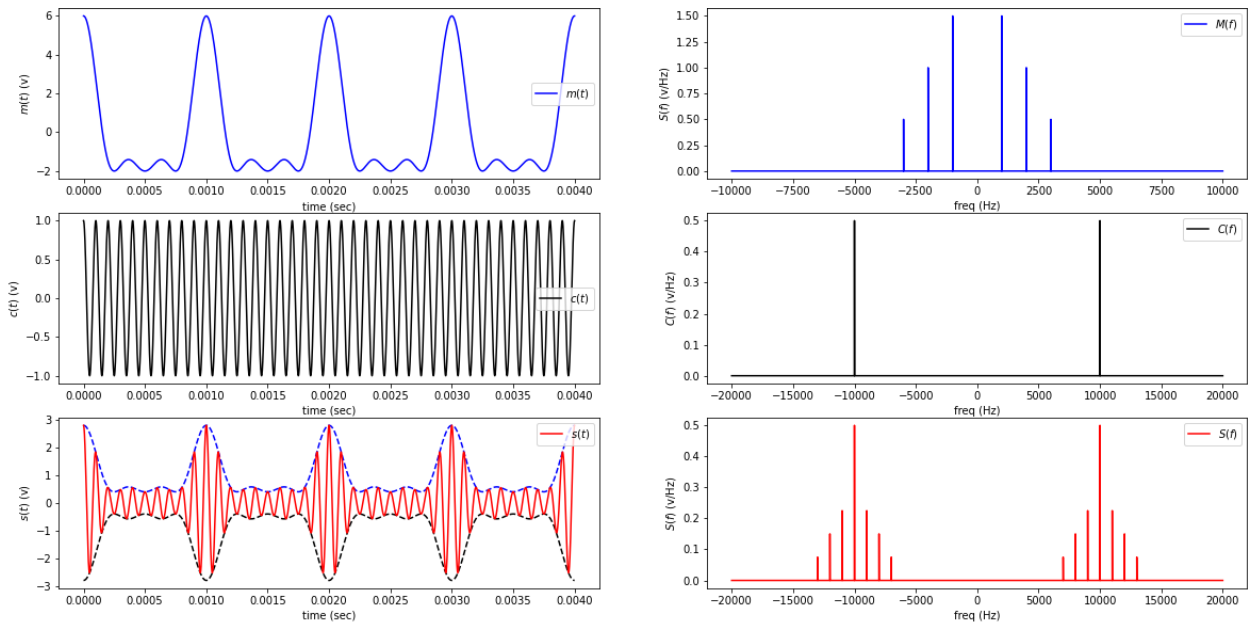


Figure 9: Normal AM modulation of a message signal with multiple harmonics

- Note:** We notice 3 signal in the above figure, $m(t)$ -message- that contains 3 message signals (3 cos), $c(t)$ - carrier - each with a different shape, amplitude and frequency. $S(t)$ –AM modulation signal- signal That depend on $m(t)$ and $c(t)$.

Exercise:

1- $f_{m1}=500$, $f_{m2}=1000$, $f_{m3}=1500$:

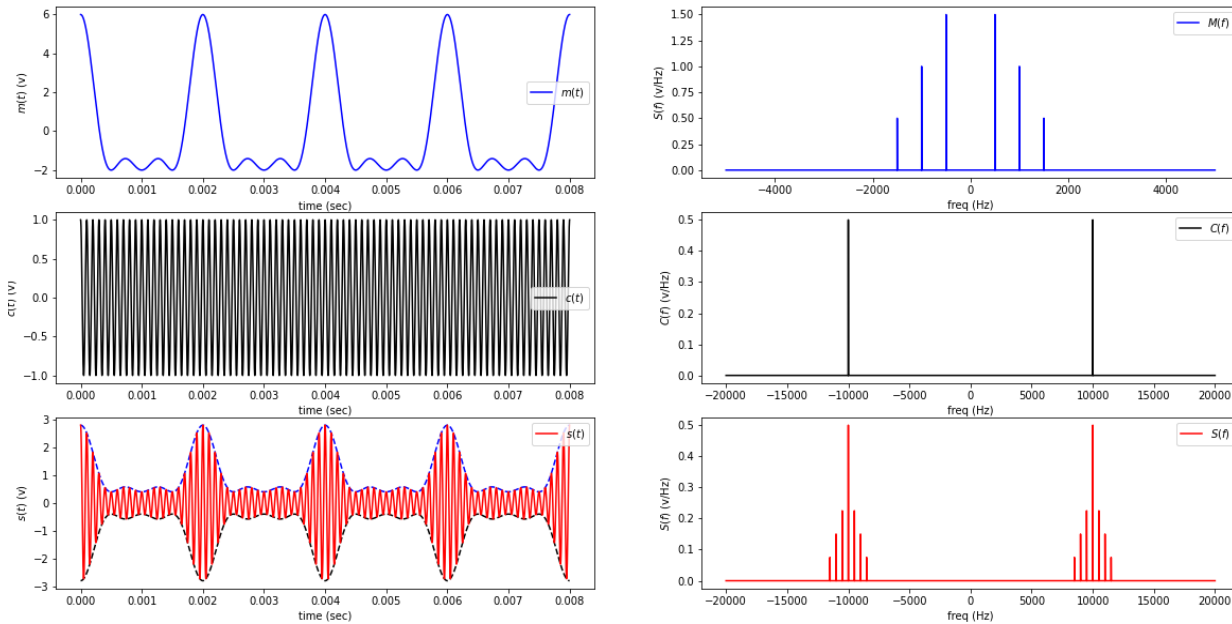


Figure 10: Normal AM modulation of a message signal with multiple harmonics($f_{m1}=500, f_{m2}=1000, f_{m3}=1500$)

- Note:** when f_m was change the waves for message change . also the carrier envelop and AM signal waves expand and move away from each other if f_m decreased or close together if f_m increase. in addition to the AM signal frequency between the carrier frequency changed by :
 $(f_c - f_m, f_c, f_c + f_m)$ and $(-f_c - f_m, -f_c, -f_c + f_m)$
 But the carrier frequency doesn't change.

2- $f_c=8000$ Hz

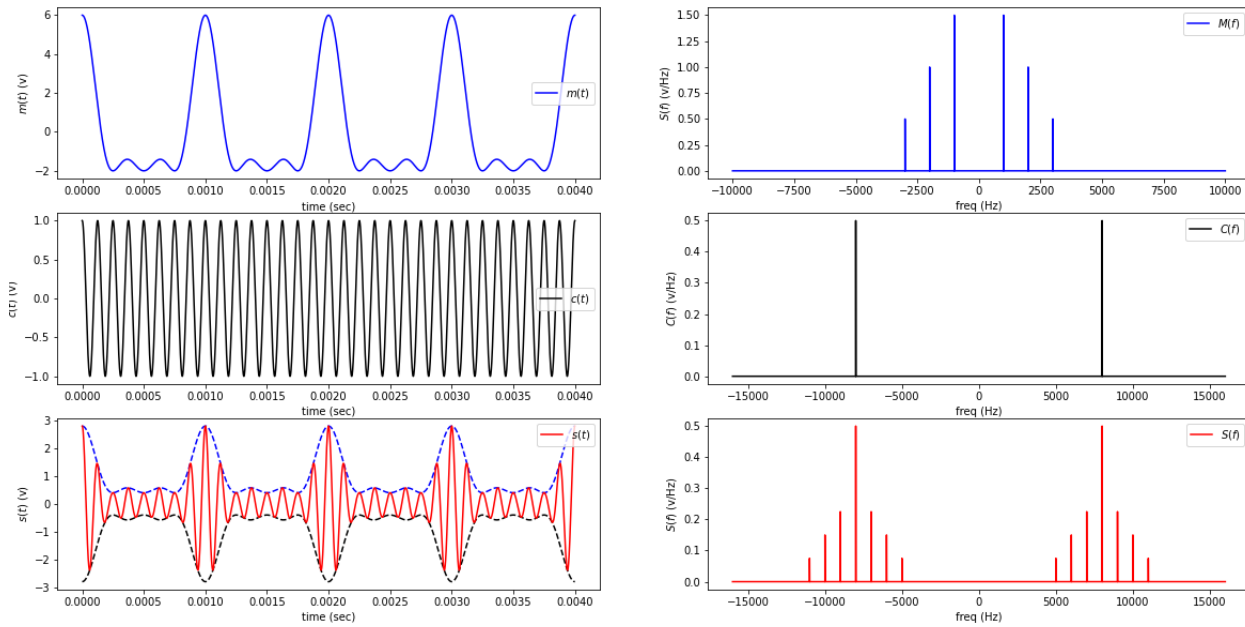


Figure 11: Normal AM modulation of a message signal with multiple harmonics $f_c=8000$

- Note:** when f_c was decreased/increase the envelop and frequency of message signal were not affected . but waves for carrier envelop and AM signal waves expand and move away from each other if decreased or close together if increase . And the AM signal frequency changed by: $(f_c - f_m, f_c, f_c + f_m)$, $(-f_c - f_m, -f_c, -f_c + f_m)$.

3- $A_{m1}=2$, $A_{m2}=4$, $A_{m3}=0$

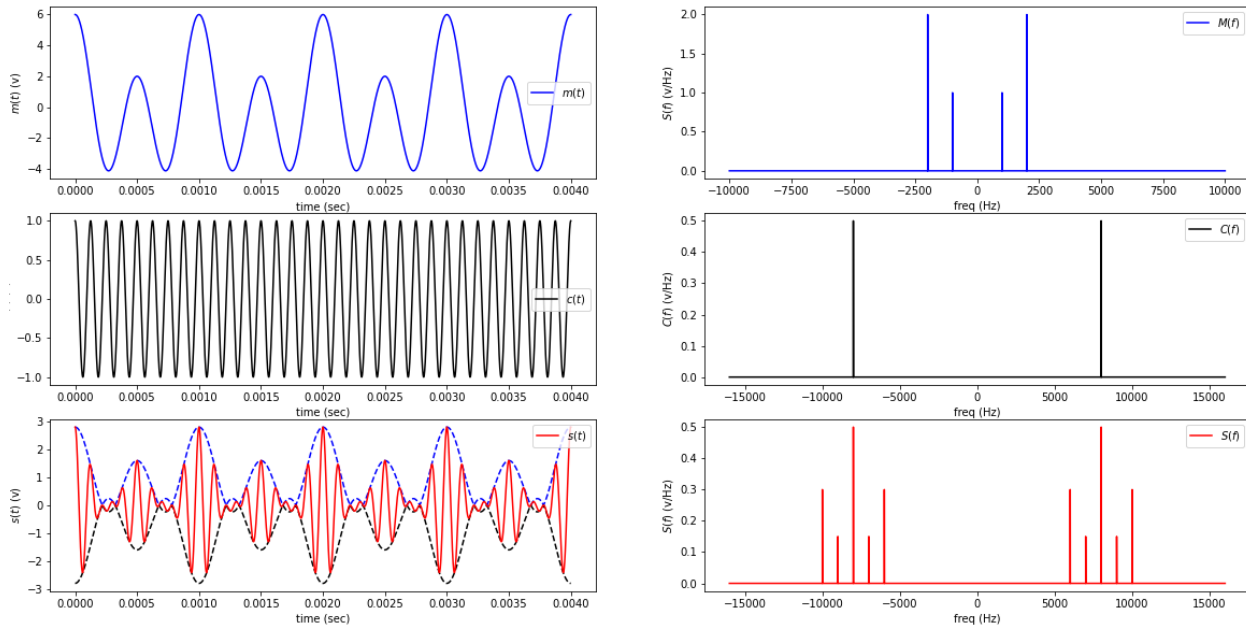
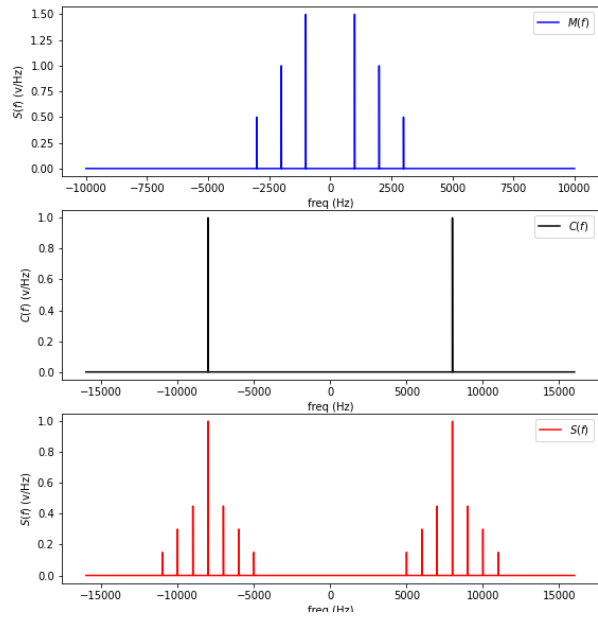
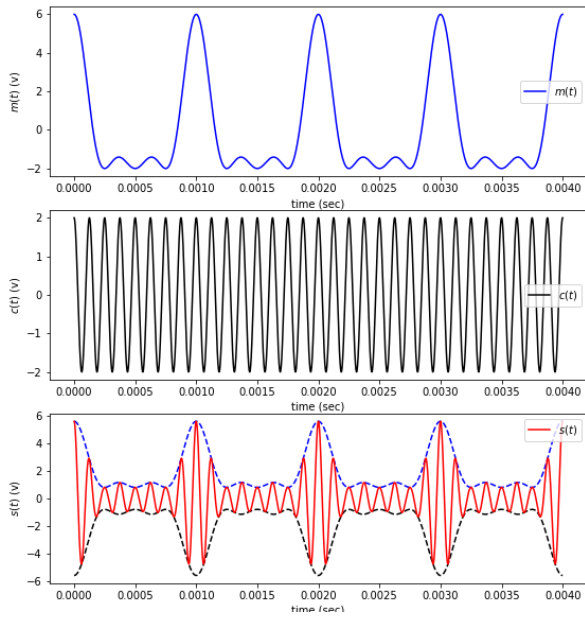


Figure 12: Normal AM modulation of a message signal with multiple harmonics($A_{m1}=2, A_{m2}=4, A_{m3}=0$)

- Note:** At the beginning, we notice when we put ($A_{m3}=0$) this message (m_3) has disappeared. Also, when A_m increased the peak of the message increases and AM signals envelope increases by $(A_c + (A_c \cdot A_m \cdot K_a))$. in addition to, message amplitude frequency value changes by $(A_m/2)$ also for the upper and lower parts in AM frequency change by $(A_m \mu/4)$. but the carrier envelop and frequency were not affected.

4- $A_c=2$



- **Note:** when A_c increase/decreases the peak of the carrier increases/decreases and AM signals envelope increases/decreases by $(A_c + (A_c \cdot A_m \cdot K_a))$. in addition to, carrier amplitude frequency value changes by $(A_c/2)$. But the message envelope and frequency doesn't change.

❖ Part 4: Demodulation of Normal AM:

$$1/f_c < 1/\tau < 1/f_m$$

Where:

f_m: frequency of message signal
f_c: frequency of carrier signal
τ: discharging time of capacitor

Let:

A_m=0.5 # amplitude of message signal
f_m=100 # frequency of message signal
A_c=1 # amplitude of carrier signal
f_c=1000 # frequency of carrier signal
K_a=1 # amplitude sensitivity
τ =3/1000

An envelope detector with capacitor was used to demodulate the Am signal. As shown in fig below.

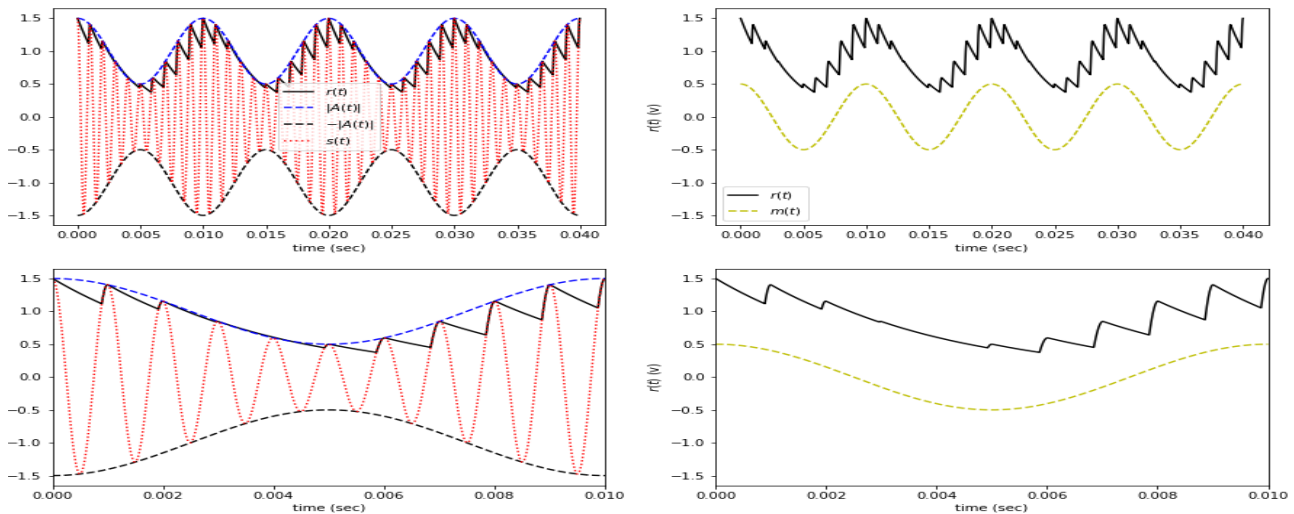


Figure 13: demodulation of Am using envelope detector

- **Note:**

$S(t)$: message signal.

$-|A(t)|$: negative envelop

$|A(t)|$: positive envelop

$r(t)$: recovered signal

Exercise:

1- a) $\tau = 10/1000$

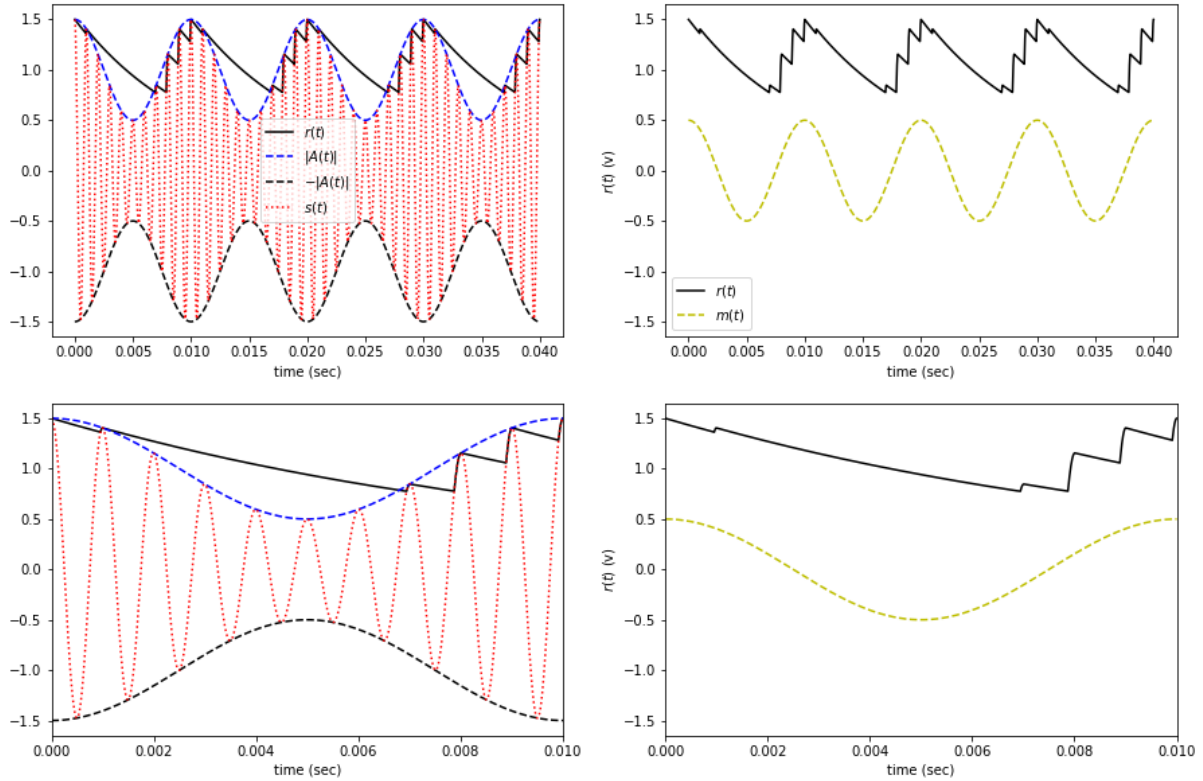


Figure 14: demodulation of Am using envelope detector with $\tau = 10/1000$

- **Note:** when increases τ the capacitor discharging slowly And it is not able to follow the envelop of AM signal .

b) $\tau = 1/1000$

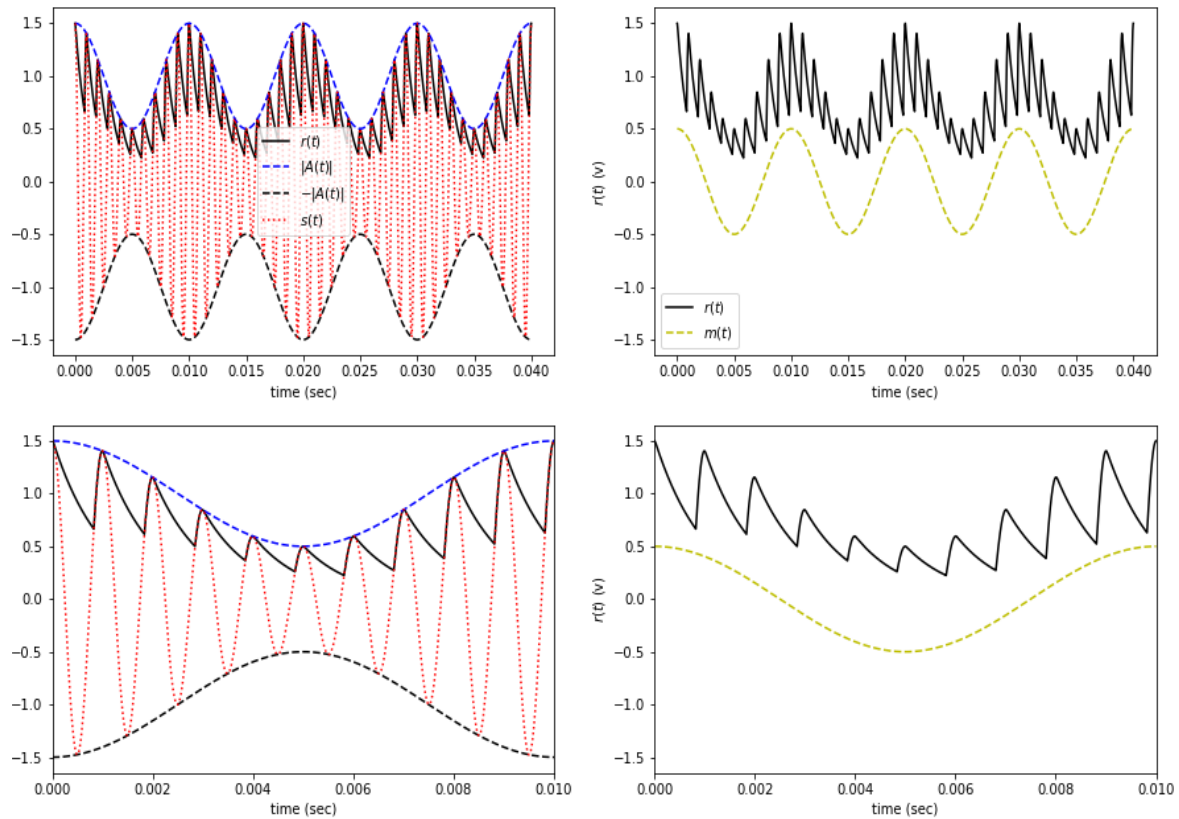


Figure 15: demodulation of Am using envelope detector with $\tau = 1/1000$

- **Note:** when decrease the magnitude of τ , discharging time fast But this thing is not good because of the ripple is sharp And it is not able to follow the envelop of AM signal.

c) $\tau = 4/1000$

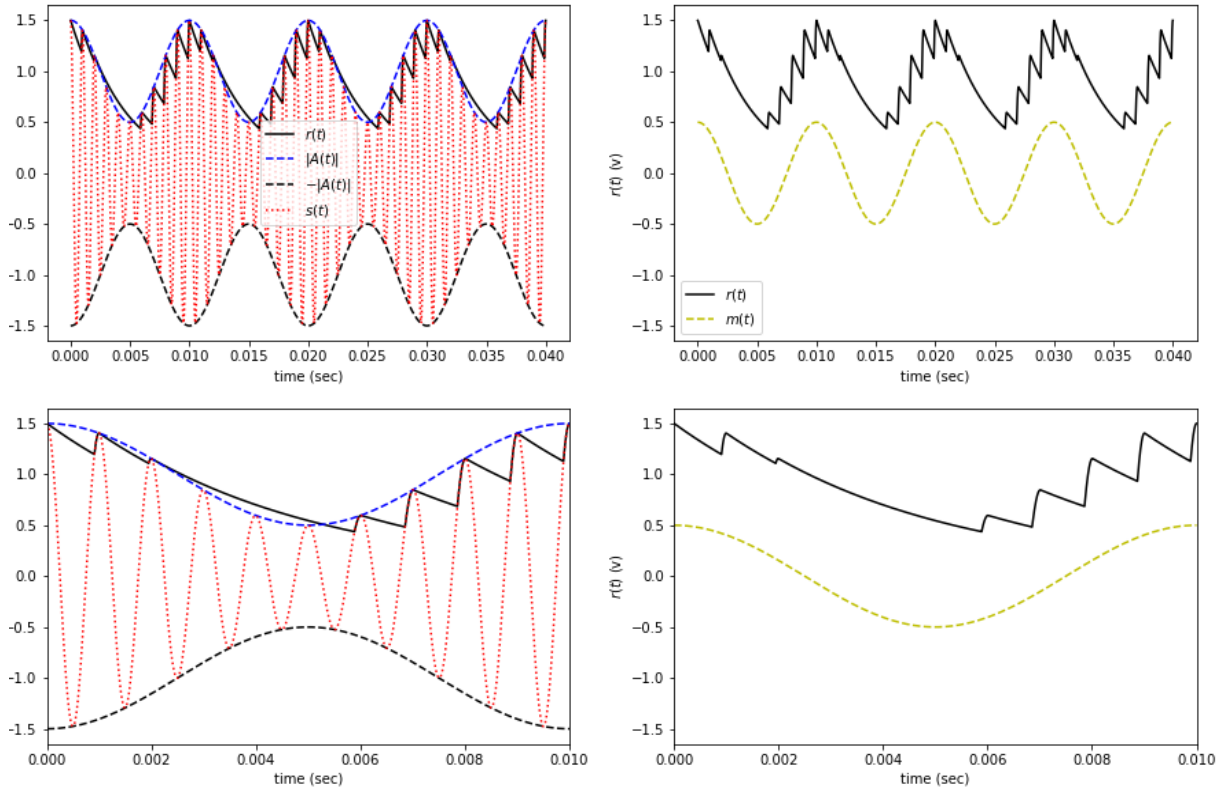


Figure 16: demodulation of Am using envelope detector with $\tau = 4/1000$

- **Note:** when chose value of τ between $1/f_c$ and $1/f_m$ this thing good And the ripple able to follow the envelop of AM signal.

2- $f_c=500$ Hz

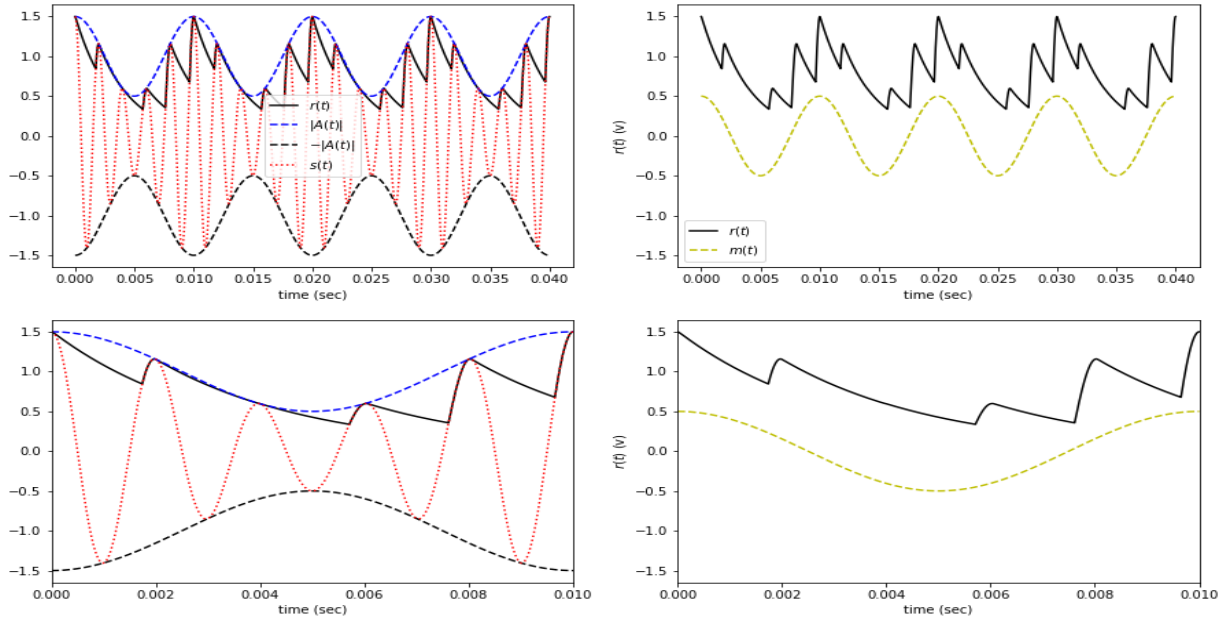


Figure 17: demodulation of Am using envelope detector with $f_c = 500$ hz

3- $f_m=50$ Hz

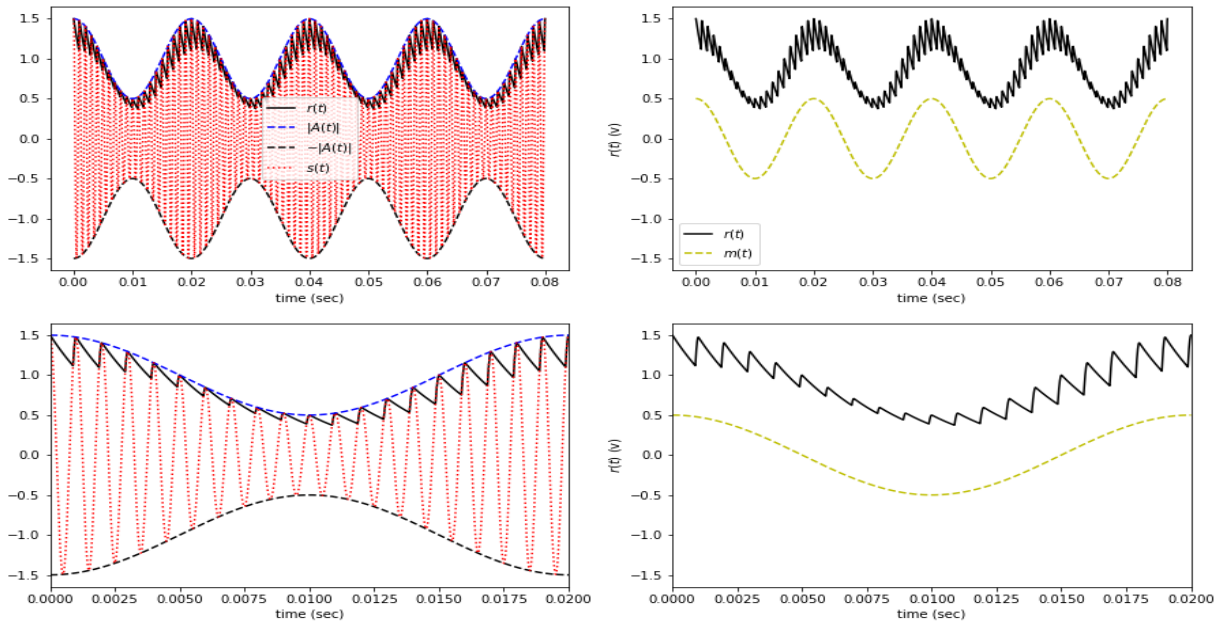


Figure 18: demodulation of Am using envelope detector with $f_m = 50$ hz

- **Note:** when f_c decreases the ripple increases and when f_m decreases the signal becomes moother because we modulated a smaller signal.

4- $K_a = 0.5$

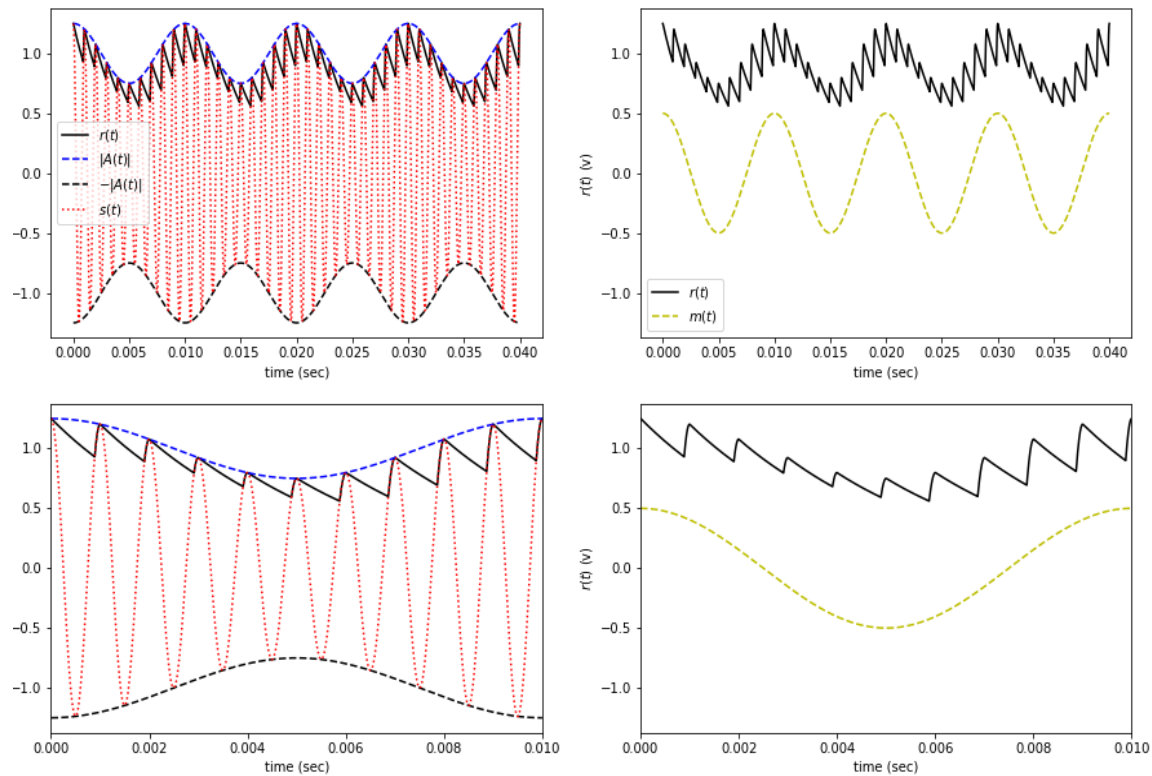


Figure 19: demodulation of Am using envelope detector with $K_a = 0.5$

- Note:** The constant K_a is the amplitude sensitivity of the modulator or the transmitter. The percentage of modulation will depend on the absolute value of $K_a \cdot m(t)$. If the absolute value of $K_a \cdot m(t)$ is less or equal to 1 for all t , then the percentage of modulation is less than or equal to 100%. However, if the absolute value of $K_a \cdot m(t)$ is greater than 1 for some t , then the percent of modulation is in excess of 100% or over modulation.